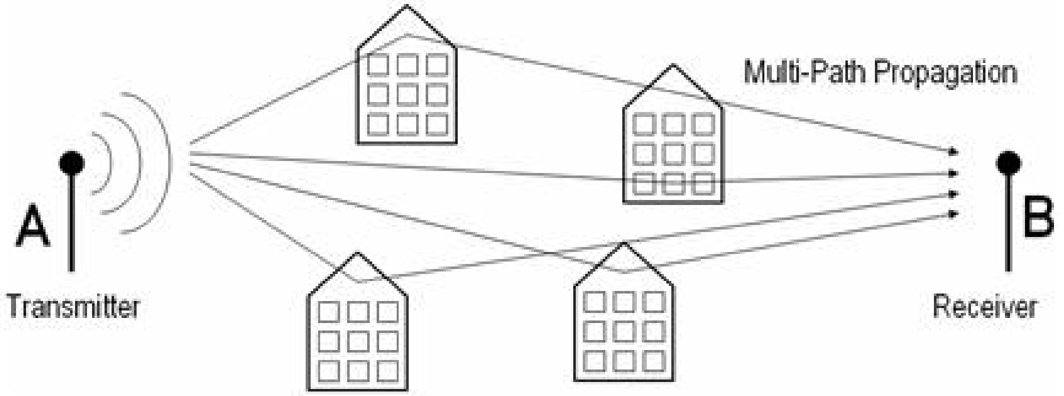
Introduction to Wireless Signal Propagation



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Audio/Video recordings of this class lecture are available at:
http://www.cse.wustl.edu/~jain/cse574-20/

Student Questions

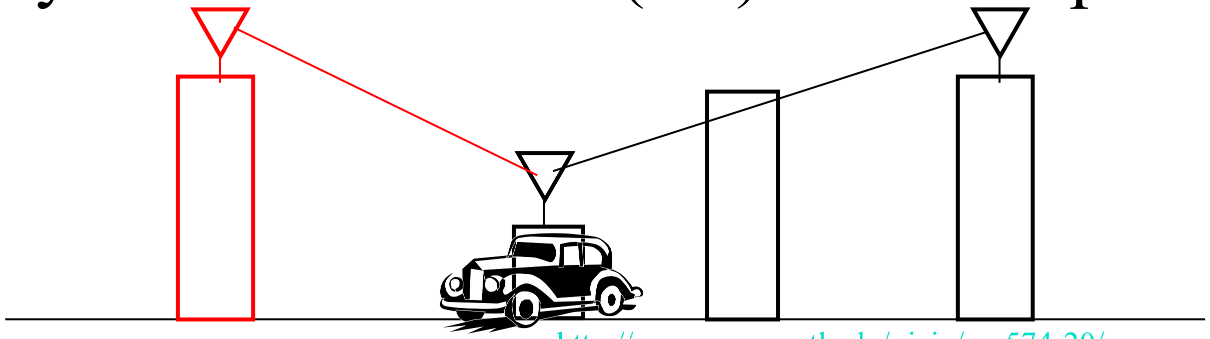
1. Reflection, Diffraction, Scattering
2. Fading, Shadowing, multipath
3. Fresnel Zones
4. Multi-Antenna Systems, Beam forming, MIMO
5. OFDM

Note: This is the 2nd in a series of 2 lectures on wireless physical layer. Modulation, coding, Shannon's theorem, etc were discussed in the other lecture.

Student Questions

Wireless Radio Channel

- Path loss: Depends upon distance and frequency
- Noise
- Shadowing: Obstructions
- Frequency Dispersion (Doppler Spread) due to motion
- Interference
- Multipath: Multiple reflected waves
- Inter-symbol interference (ISI) due to dispersion

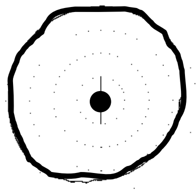


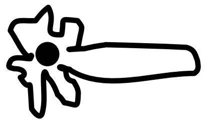
Student Questions

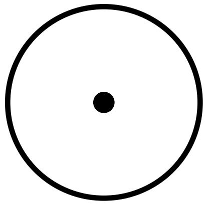
Antenna

- Transmitter converts electrical energy to electromagnetic waves
- Receiver converts electromagnetic waves to electrical energy
- Same antenna is used for transmission and reception
- Omni-Directional: Power radiated in all directions
- Directional: Most power in the desired direction
- Isotropic antenna: Radiates in all directions equally
- Antenna Gain = Power at particular point/Power with Isotropic
  Expressed in dBi

$$P_r = P_t G_t G_r (\lambda/4\pi d)^2$$

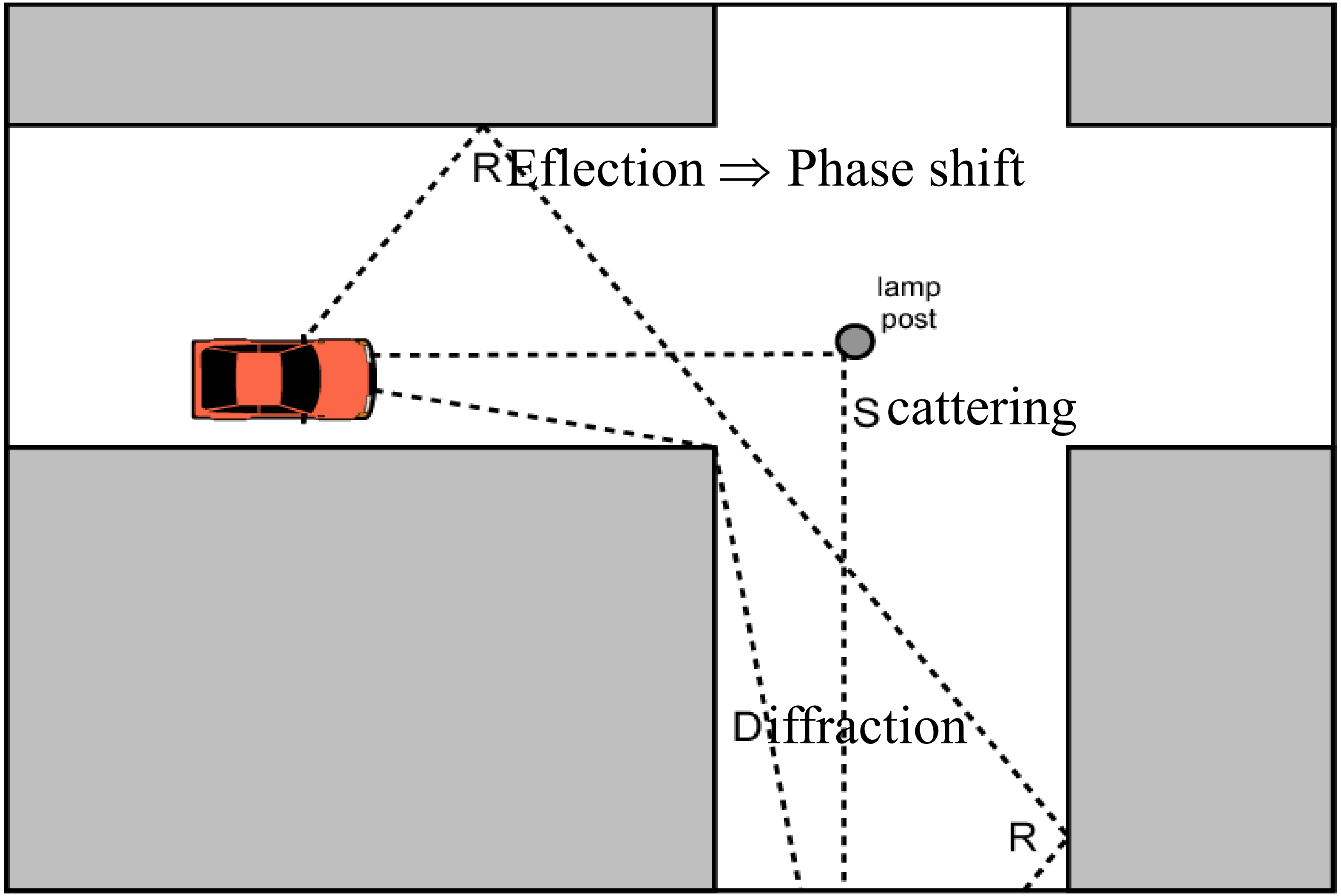

Omni-Directional


Directional


Isotropic

Student Questions

Reflection, Diffraction, Scattering



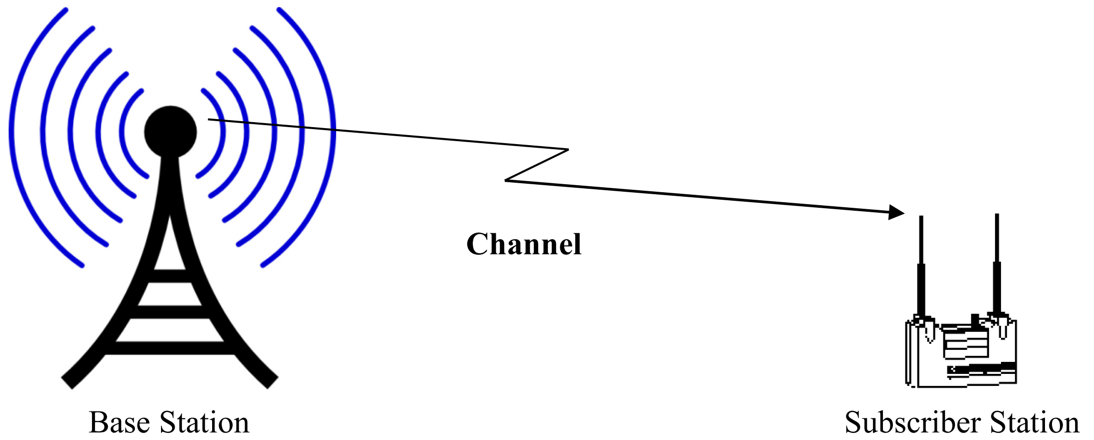
Student Questions

Reflection, Diffraction and Scattering (Cont)

- **Reflection**: Surface large relative to wavelength of signal
  - May have phase shift from original
  - May cancel out original or increase it
- **Diffraction**: Edge of impenetrable body that is large relative to λ
  - May receive signal even if no line of sight (LOS) to transmitter
- **Scattering**
  - Obstacle size on order of wavelength. Lamp posts etc.
- If LOS, diffracted and scattered signals not significant
  - Reflected signals may be
- If no LOS, diffraction and scattering are primary means of reception

Student Questions

Channel Model



- Power profile of the received signal can be obtained by *convolving* the power profile of the transmitted signal with the impulse response of the channel.
- Convolution in time = multiplication in frequency
- Signal x, after propagation through the channel H becomes y:

$$y(f)=H(f)x(f)+n(f)$$

- Here $H(f)$ is **channel response**, and $n(f)$ is the noise. Note that x, y, H, and n are all functions of the signal frequency f.

Student Questions

Path Loss

- Power is distributed equally to spherical area $4\pi\ d^2$
- The received power depends upon the wavelength
- If the Receiver collects power from area A_R:

$$P_R = P_T G_T \frac{1}{4\pi d^2} A_R$$

- Receiving Antenna Gain

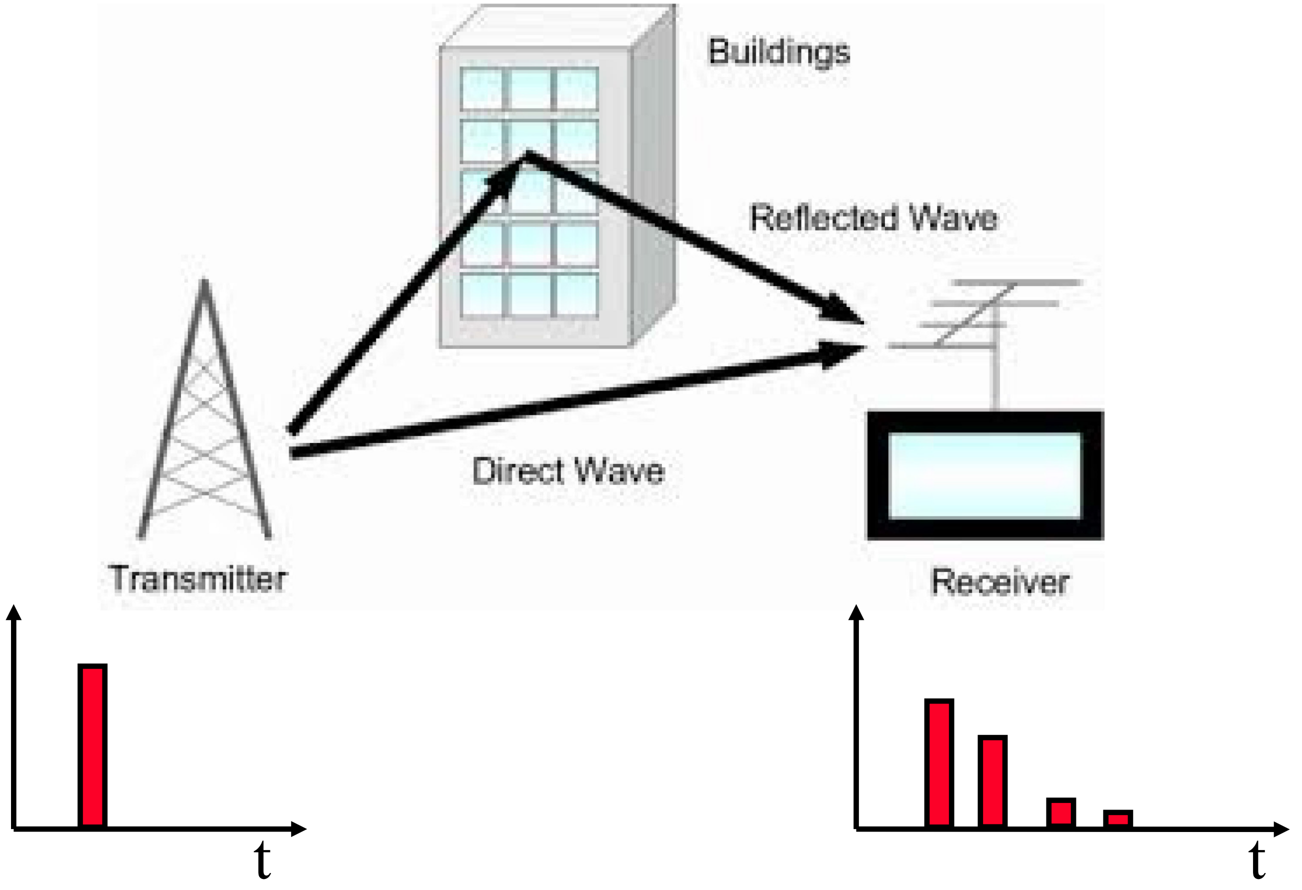
$$G_R = \frac{4\pi}{\lambda^2} A_R$$

$$P_R = P_T G_T G_R \left(\frac{\lambda}{4\pi d}\right)^2$$

- This is known as **Frii's Law**.
  Attenuation in free space increases with frequency.

Student Questions

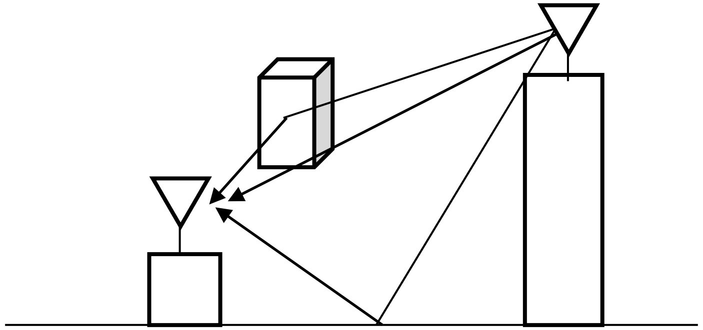
Multipath

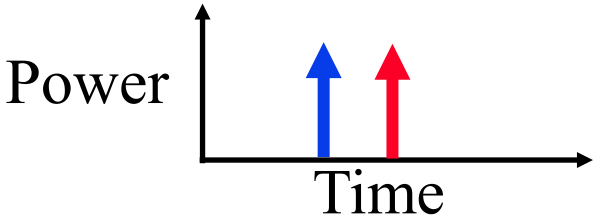


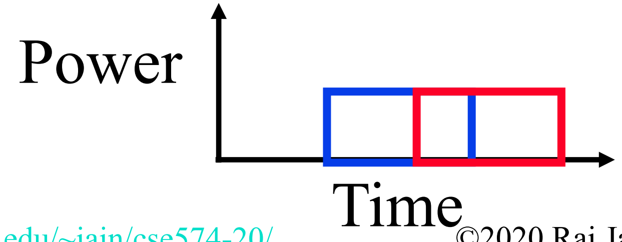
- Multiple reflected copies of the signal are received

Student Questions

Inter-Symbol Interference



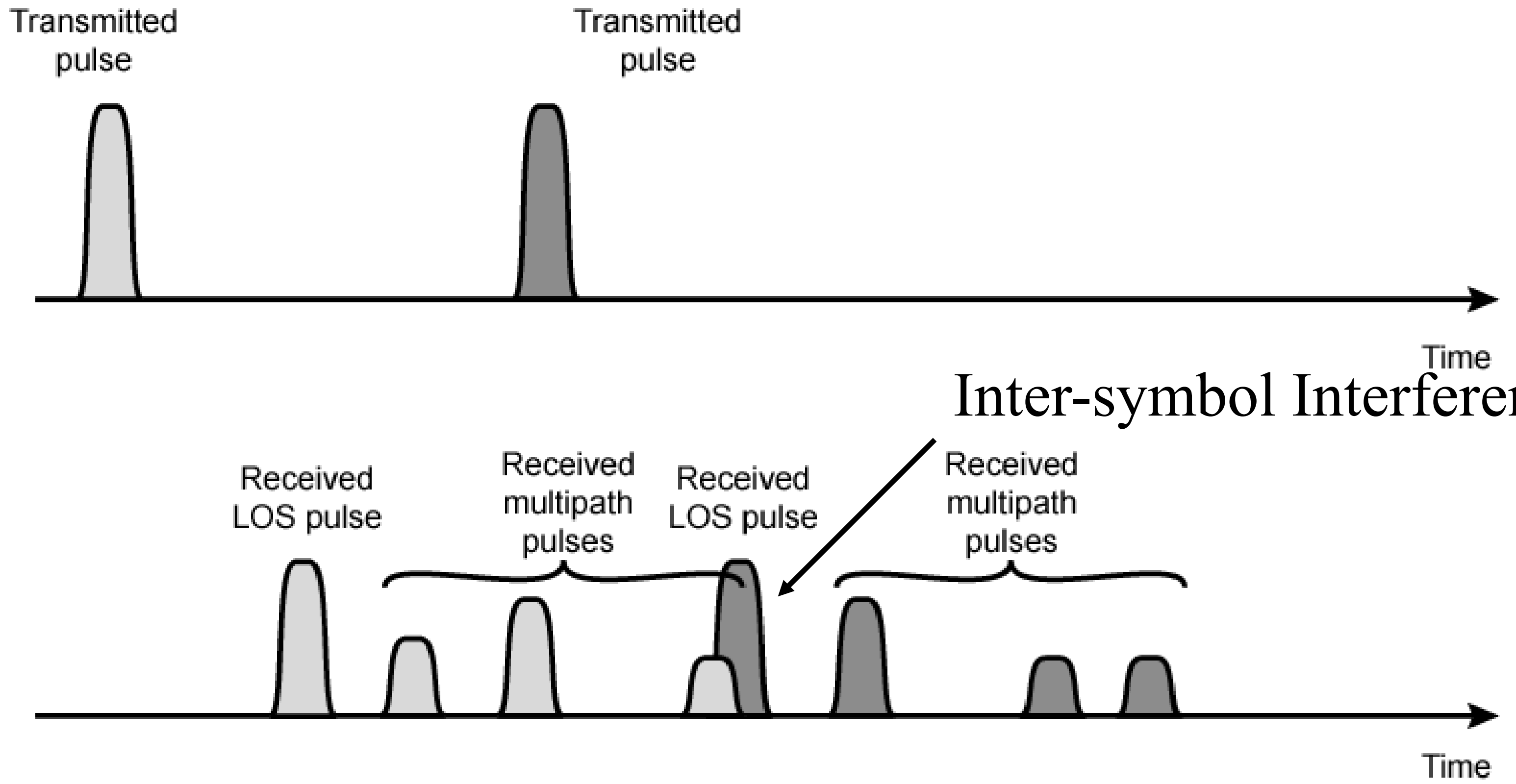




- Symbols become wider
  ⇒ Limits the number of bits/s

Student Questions

Multipath Propagation

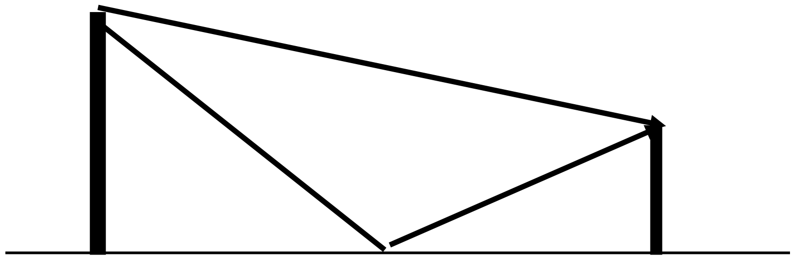


Inter-symbol Interference

- Delay Spread = Time between first and last versions of signal
- Fading: Fluctuation in amplitude, phase or delay spread
- Multipath may add constructively or destructively
  ⇒ Fast fading

Student Questions

d^{-4} Power Law



- Using a two-ray model

$$P_R = P_T G_T G_R \left(\frac{h_t h_r}{d^2}\right)^2$$

- Here, h_T and h_R are heights of transmit and receive antennas
- It is valid for distances larger than

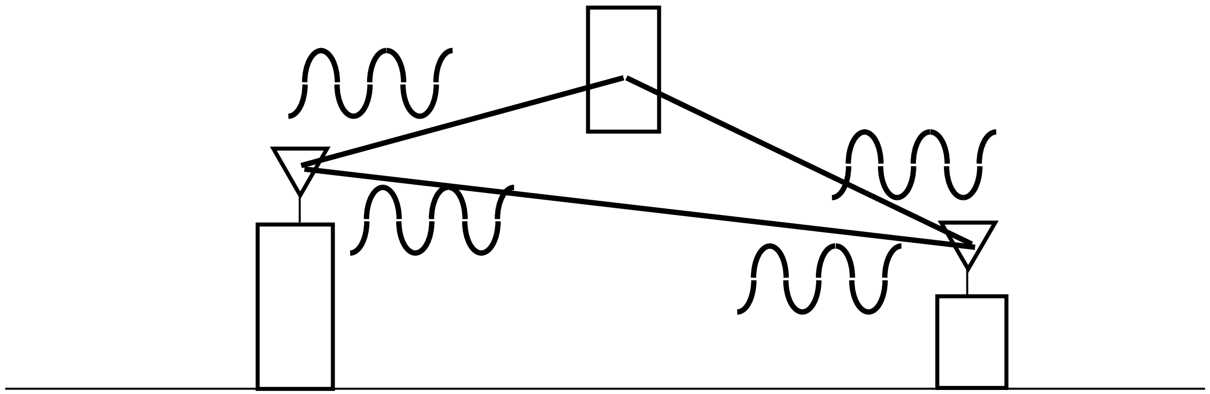
$$d_{\text{break}} = 4 h_T h_R / \lambda$$

- Note that the received power becomes independent of the frequency.
- Measured results show n=1.5 to 5.5. Typically 4.

Student Questions

Small Scale Fading

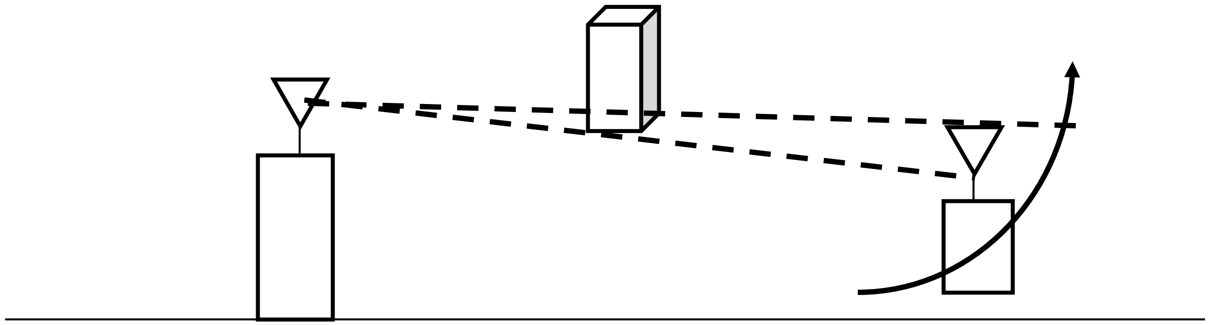
- The signal amplitude can change by moving a few inches ⇒ Small scale fading

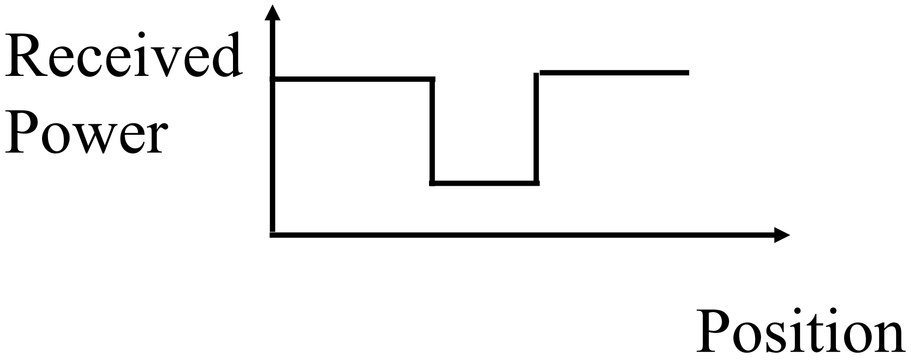


Student Questions

Shadowing

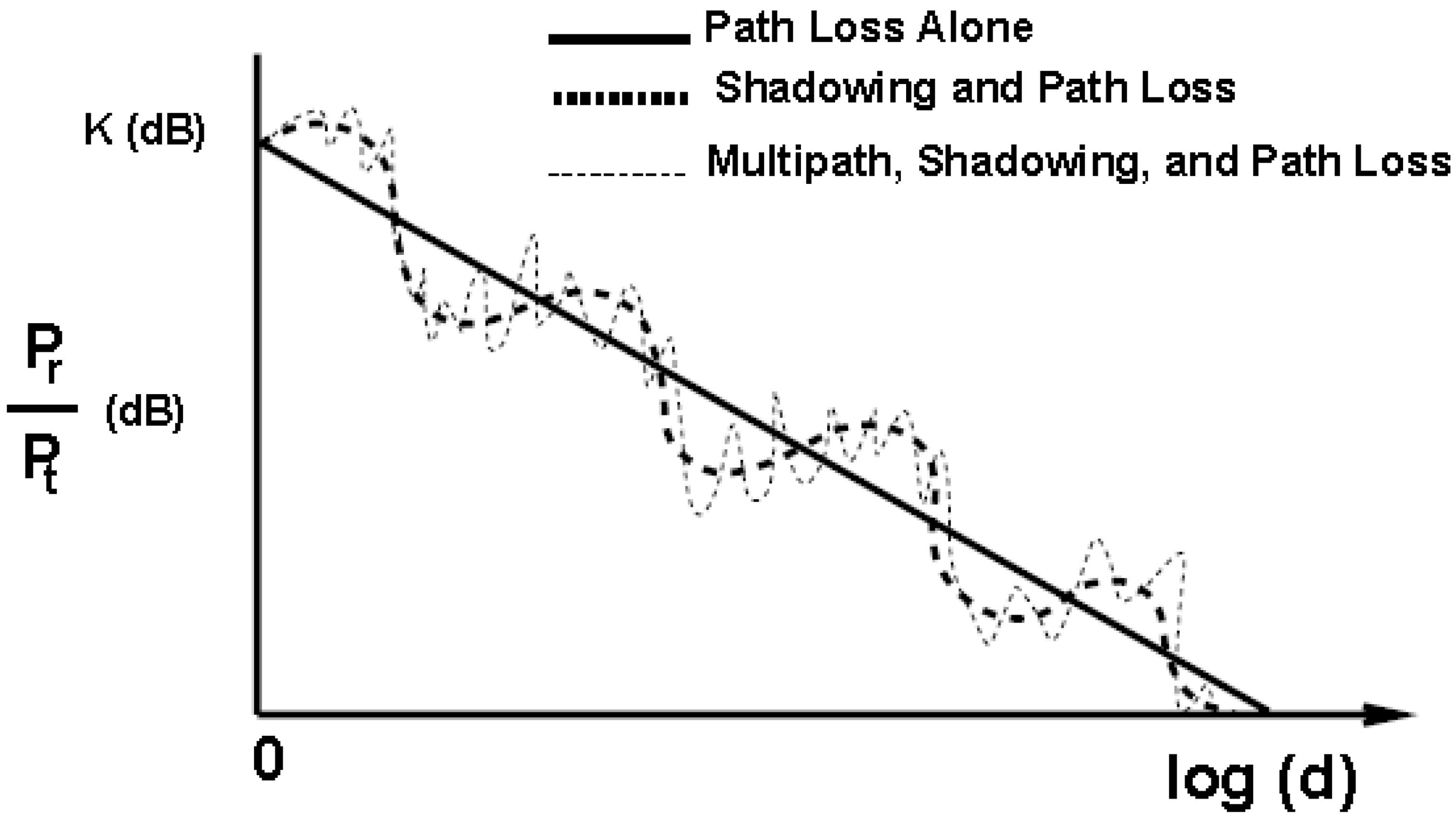
- Shadowing gives rise to large scale fading





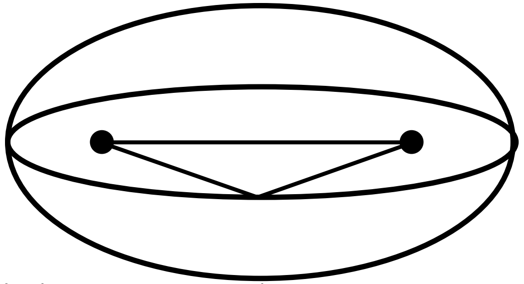
Student Questions

Total Path Loss



Student Questions

Fresnel Zones



- Draw an ellipsoid with BS and MS as Foci
- All points on ellipsoid have the same BS-MS run length
- Fresnel ellipsoids = Ellipsoids for which run length = LoS + $i\lambda/2$
- At the Fresnel ellipsoids results in a phase shift of $i\pi$
- Radius of the i^{th} ellipsoid at distance d_T from the transmitter and d_R from the receiver is $\sqrt{\frac{i\lambda d_T d_R}{d_T + d_R}}$
- Free space (d^2) law is followed up to the distance at which the first Fresnel Ellipsoid touches the ground

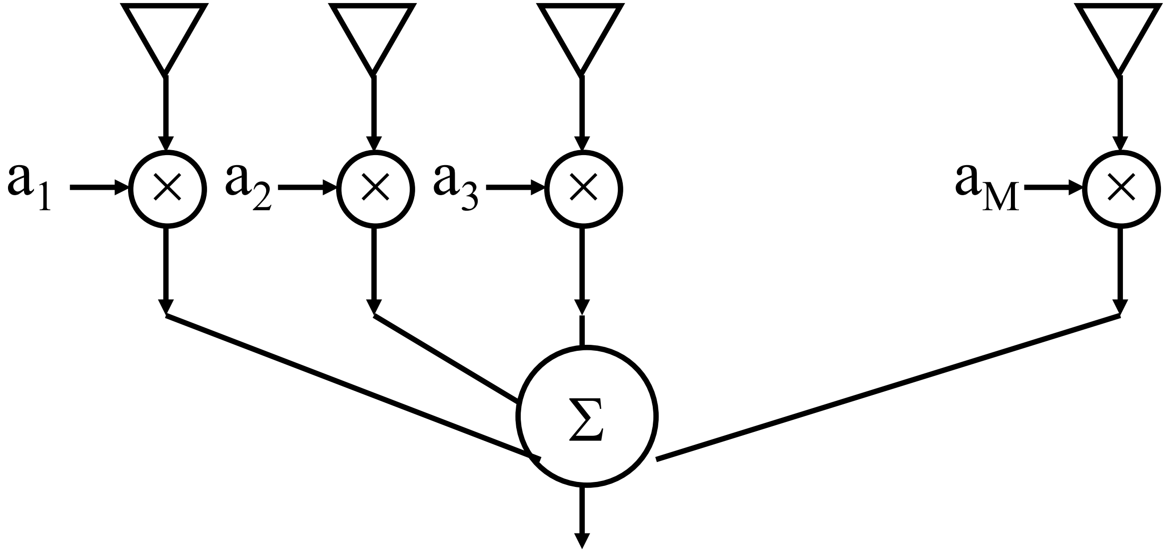
Student Questions

Multi-Antenna Systems

- Receiver Diversity
- Transmitter Diversity
- Beam forming
- MIMO

Student Questions

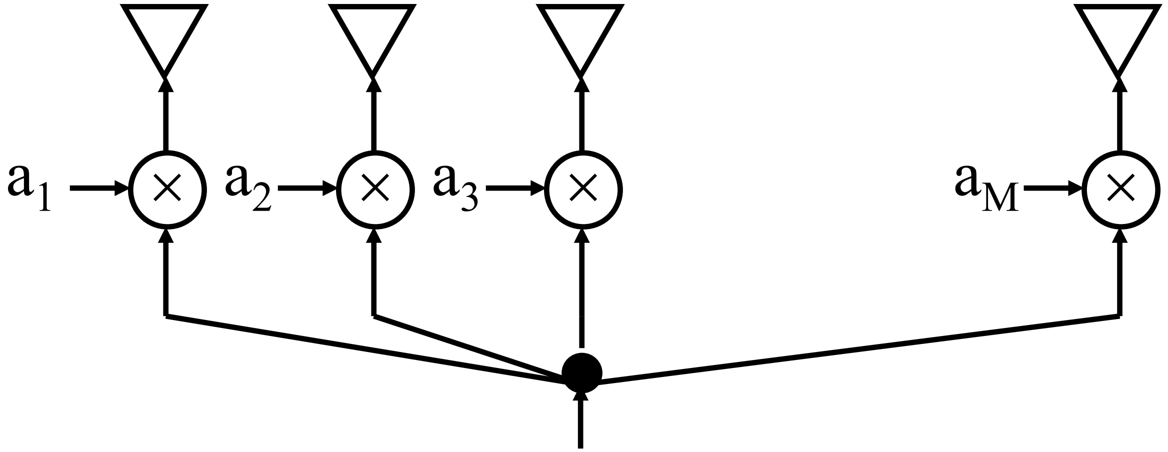
Receiver Diversity



- User multiple receive antenna
- Selection combining: Select antenna with highest SNR
- Threshold combining: Select the first antenna with SNR above a threshold
- Maximal Ratio Combining: Phase is adjusted so that all signals have the same phase. Then weighted sum is used to maximize SNR

Student Questions

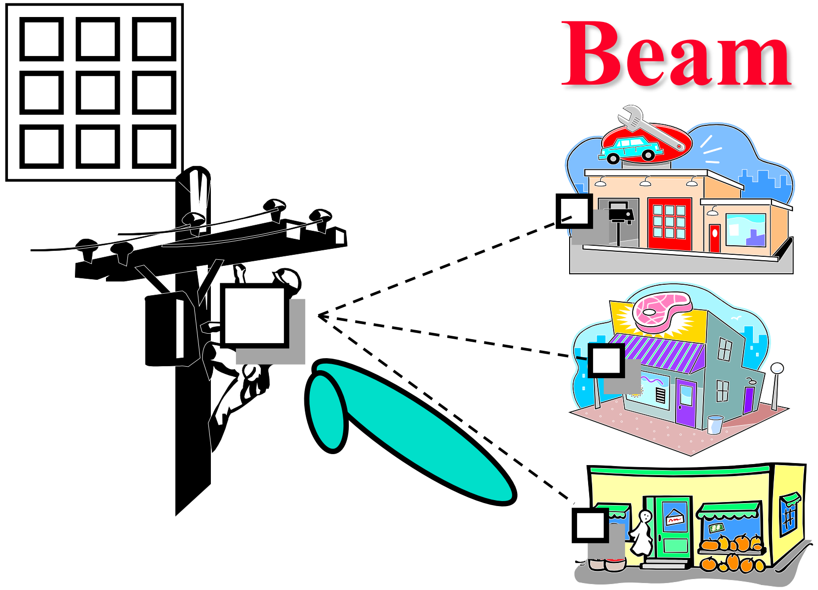
Transmitter Diversity



- Use multiple antennas to transmit the signal
  Ample space, power, and processing capacity at the transmitter (but not at the receiver).
- If the channel is known, phase each component and weight it before transmission so that they arrive in phase at the receiver and maximize SNR
- If the channel is not known, use space time block codes

Student Questions

Beam forming

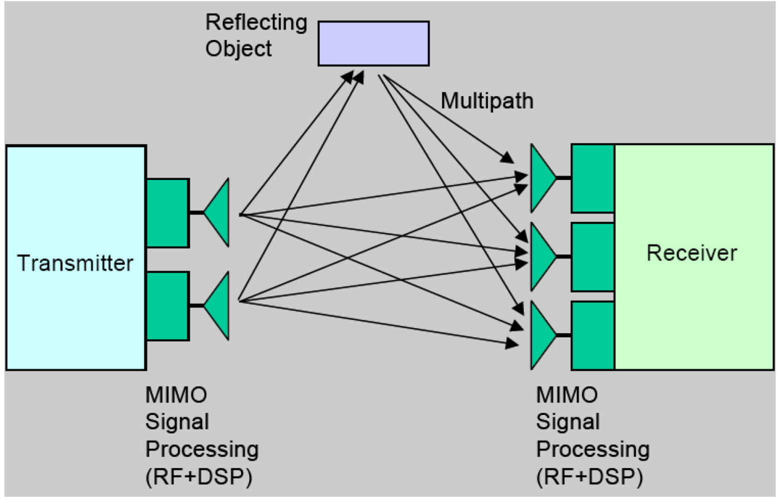


- Phased Antenna Arrays:
  Receive the same signal using multiple antennas
- By phase-shifting various received signals and then summing ⇒ Focus on a narrow directional beam
- Digital Signal Processing (DSP) is used for signal processing ⇒ Self-aligning

Student Questions

MIMO

- Multiple Input Multiple Output
- RF chain for each antenna
  ⇒ Simultaneous reception or transmission of multiple streams



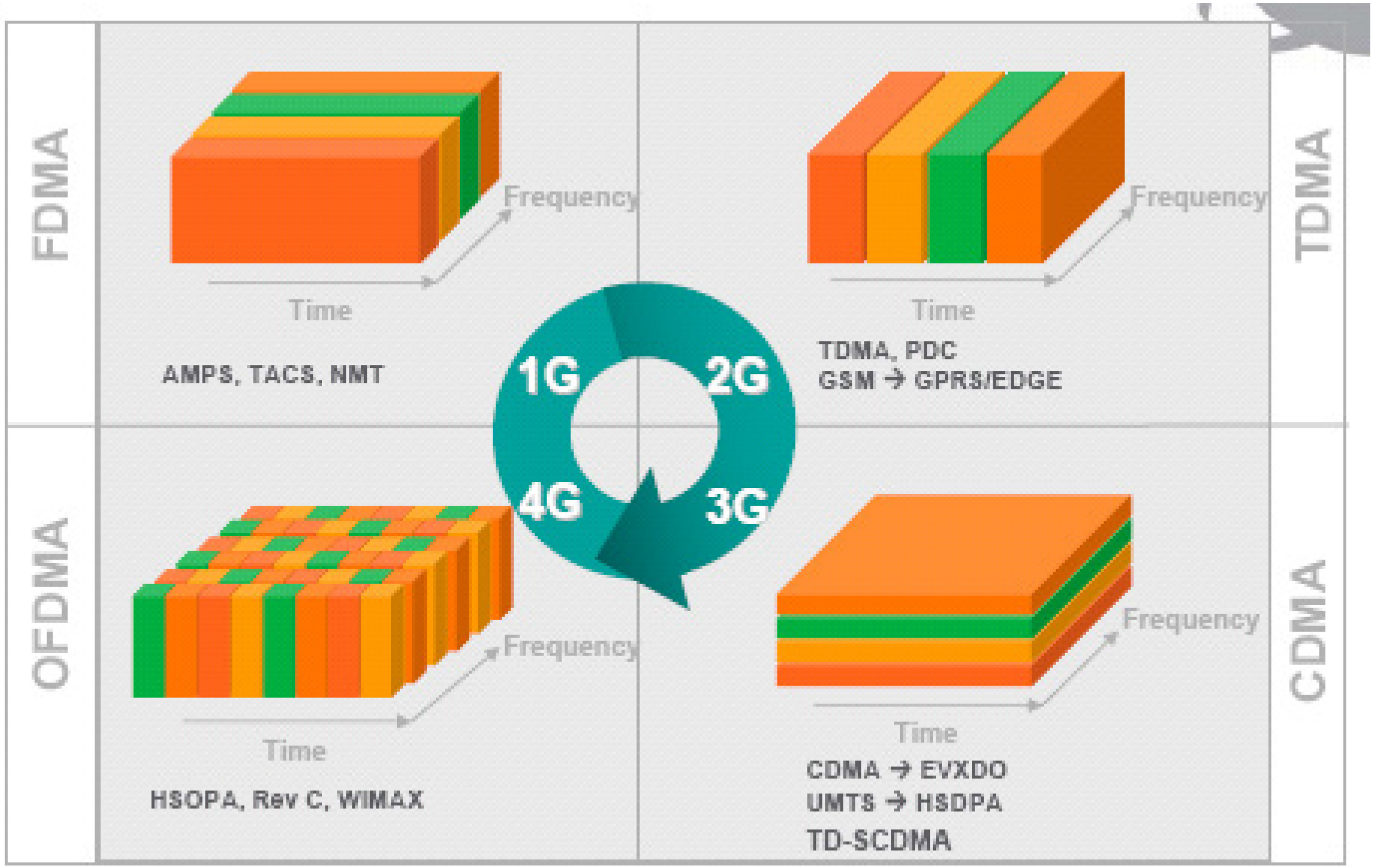
2x3

802.16e at 2.5 GHz, 10 MHz TDD, D:U=2:1

T:R	1x1	1x2	2x2	2x4	4x2	4x4
b/Hz	1.2	1.8	2.8	4.4	3.7	5.1

Student Questions

Multiple Access Methods

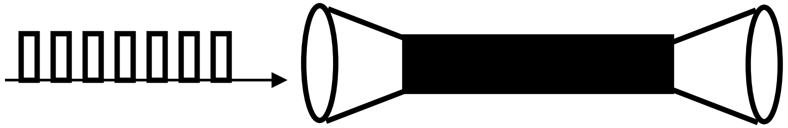


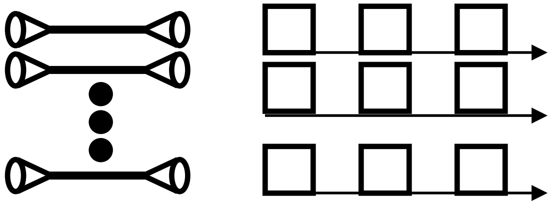
Source: Nortel

Student Questions

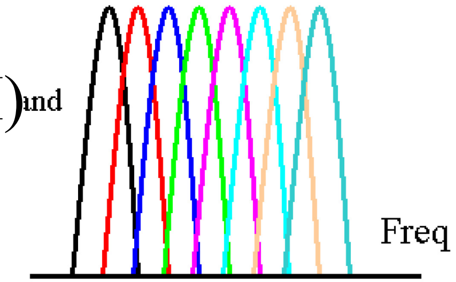
OFDM

- Orthogonal Frequency Division Multiplexing
- Ten 100 kHz channels are better than one 1 MHz Channel
  ⇒ Multi-carrier modulation

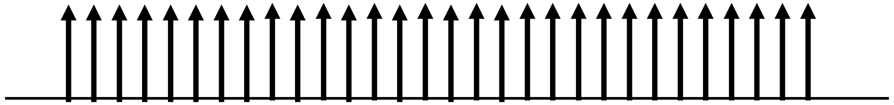




- Frequency band is divided into 256 or more sub-bands.
  Orthogonal ⇒ Peak of one at null of others
- Each carrier is modulated with a BPSK, QPSK, 16-QAM, 64-QAM etc depending on the noise (Frequency selective fading)
- Used in 802.11a/g, 802.16,
  Digital Video Broadcast handheld (DVB-H)



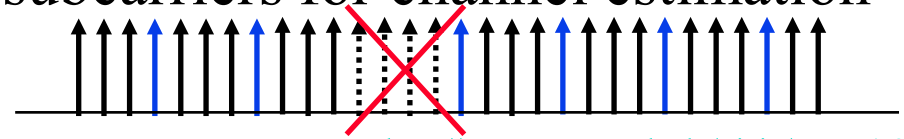
- Easy to implement using FFT/IFFT



Student Questions

Advantages of OFDM

- Easy to implement using FFT/IFFT.
  FFT/IFFT are implemented only as powers of 2 (256, 1024, …)
- Computational complexity = O(B log BT) compared to previous $O(B^2T)$ for Equalization. Here B is the bandwidth and T is the delay spread.
- Graceful degradation if excess delay
- Robustness against frequency selective burst errors
- Allows adaptive modulation and coding of subcarriers
- Robust against narrowband interference (affecting only some subcarriers)
- Allows pilot subcarriers for channel estimation



Student Questions

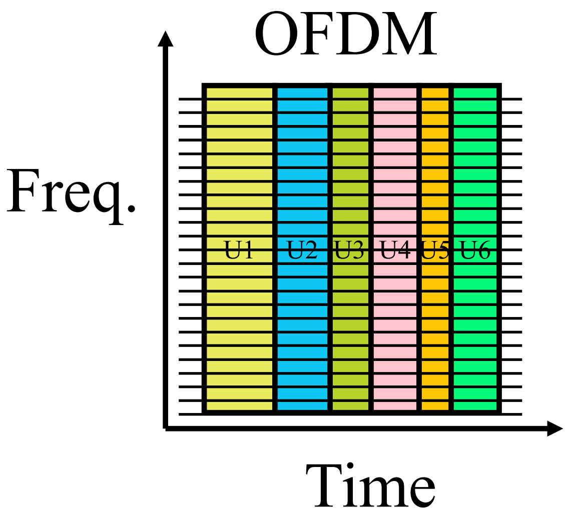
OFDM: Design considerations

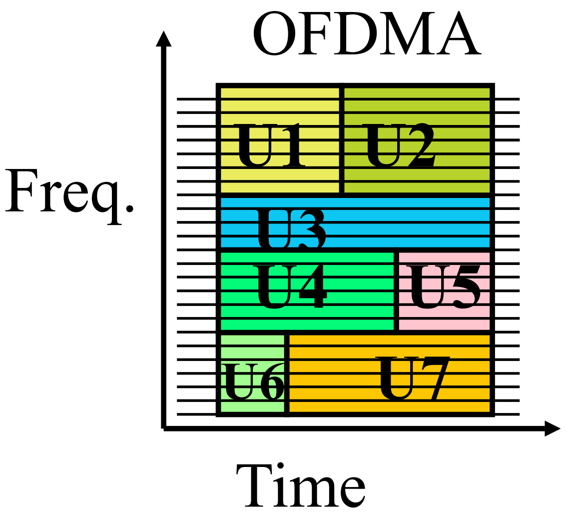
- Large number of carriers ⇒ Smaller data rate per carrier ⇒ Larger symbol duration ⇒ Less inter-symbol interference
- Reduced subcarrier spacing ⇒ Increased inter-carrier interference due to Doppler spread in mobile applications
- Easily implemented as Inverse Discrete Fourier Transform (IDFT) of data symbol block
- Fast Fourier Transform (FFT) is a computationally efficient way of computing DFT

Student Questions

OFDMA

- Orthogonal Frequency Division Multiple Access
- Each user has a subset of subcarriers for a few slots
- OFDM systems use TDMA
- OFDMA allows Time+Freq DMA ⇒ 2D Scheduling



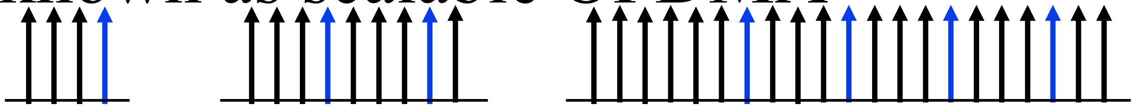


Student Questions

Scalable OFDMA (SOFDMA)

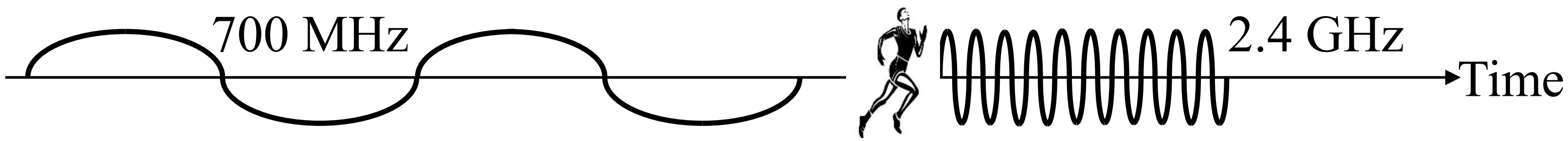
- OFDM symbol duration = f(subcarrier spacing)
- Subcarrier spacing = Frequency bandwidth/Number of subcarriers
- Frequency bandwidth=1.25 MHz, 3.5 MHz, 5 MHz, 10 MHz, 20 MHz, etc.
- Symbol duration affects higher layer operation
  - ⇒ Keep symbol duration constant at 102.9 us
  - ⇒ Keep subcarrier spacing 10.94 kHz
  - ⇒ Number of subcarriers ∝ Frequency bandwidth

  This is known as scalable OFDMA



Student Questions

Effect of Frequency



- Higher Frequencies have higher attenuation, e.g., 18 GHz has 20 dB/m more than 1.8 GHz
- Higher frequencies need smaller antenna
  Antenna $\geq$ Wavelength/2, 800 MHz $\Rightarrow$ 6”
- Higher frequencies are affected more by weather
  Higher than 10 GHz affected by rainfall
  60 GHz affected by absorption of oxygen molecules
- Higher frequencies have more bandwidth and higher data rate
- Higher frequencies allow more frequency reuse
  They attenuate close to cell boundaries. Low frequencies propagate far.

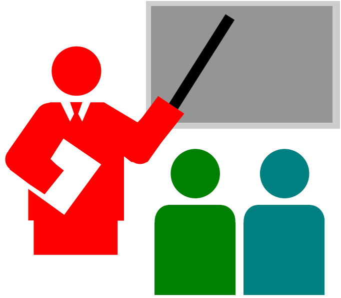
Student Questions

Effect of Frequency (Cont)

- Lower frequencies have longer reach
  ⇒ Longer Cell Radius
  ⇒ Good for rural areas
  ⇒ Smaller number of towers
  ⇒ Longer battery life
- Lower frequencies require larger antenna and antenna spacing
  ⇒ MIMO difficult particularly on mobile devices
- Lower frequencies ⇒ Smaller channel width
  ⇒ Need aggressive MCS, e.g., 256-QAM
- Doppler shift = vf/c = Velocity ×Frequency/(speed of light)
  ⇒ Lower Doppler spread at lower frequencies
- Mobility ⇒ Below 10 GHz

Student Questions

Summary



1. Path loss increase at a power of 2 to 5.5 with distance.
2. Fading = Changes in power changes in position
3. Fresnel zones = Ellipsoid with distance of LoS+iλ/2
   Any obstruction of the first zone will increase path loss
4. Multiple Antennas: Receive diversity, transmit diversity, Smart Antenna, MIMO
5. OFDM splits a band in to many orthogonal subcarriers.
   OFDMA = FDMA + TDMA

Student Questions

Homework 4

A. Determine the mean received power at a SS. The channel between a base station at 14 m and the subscriber stations at 4m at a distance of 500m. The Transmitter and Receiver antenna gains are 10dB and 5 dB respectively. Use a power exponent of 4. Transmitted power is 30 dBm. Do All calculations using dB.

B. With a subcarrier spacing of 10 kHz, how many subcarriers will be used in a system with 8 MHz channel bandwidth and what size FFT will be used?

C. In a scalable OFDMA system, the number of carriers for 10 MHz channel is 1024. How many carriers will be used if the channel was 1.25 MHz, 5 MHz, or 8.75 MHz.

Student Questions

Reading List

- Jim Geier, "Radio Wave Fundamentals," Chapter 2 in his book "Designing and Deploying 802.11 Wireless Networks: A Practical Guide to Implementing 802.11n and 802.11ac Wireless Networks, Second Edition," Cisco Press, May 2015, 600 pp., ISBN:1-58714-430-1 (Safari Book), Chapter 2.
- Raj Jain, "Channel Models: A Tutorial," WiMAX Forum AATG, February 2007, first 7 of 21 pages, http://www.cse.wustl.edu/~jain/wimax/channel_model_tutorial.htm
- Jim Geier, "Wireless Networks first-step," Cisco Press, August 2004, 264 pp., ISBN:1-58720-111-9 (Safari Book), Chapter 3.
- Steve Rackley, "Wireless Networking Technology," Newnes, March 2007, 416 pp., ISBN:0-7506-6788-5 (Safari Book), Chapter 4.
- Stephan Jones; Ronald J. Kovac; Frank M. Groom, "Introduction to Communications Technologies, 3rd Edition," CRC Press, July 2015, 364 pp., ISBN:978-1-4987-0295-9 (Safari Book), Chapters 3 and 4.

Student Questions

Wikipedia Links

- https://en.wikipedia.org/wiki/Omnidirectional_antenna
- https://en.wikipedia.org/wiki/Antenna_gain
- https://en.wikipedia.org/wiki/Equivalent_isotropically_radiated_power
- https://en.wikipedia.org/wiki/High-gain_antenna
- https://en.wikipedia.org/wiki/Signal_reflection
- https://en.wikipedia.org/wiki/Scattering
- https://en.wikipedia.org/wiki/Path_loss
- https://en.wikipedia.org/wiki/Free-space_path_loss
- https://en.wikipedia.org/wiki/Log-distance_path_loss_model
- https://en.wikipedia.org/wiki/Multipath_propagation
- https://en.wikipedia.org/wiki/Multipath_interference
- https://en.wikipedia.org/wiki/Intersymbol_interference
- https://en.wikipedia.org/wiki/Fading
- https://en.wikipedia.org/wiki/Shadow_fading
- https://en.wikipedia.org/wiki/Fresnel_zone

Student Questions

Wikipedia Links (Cont)

- https://en.wikipedia.org/wiki/Antenna_diversity
- https://en.wikipedia.org/wiki/Beamforming
- https://en.wikipedia.org/wiki/Antenna_array_(electromagnetic)
- https://en.wikipedia.org/wiki/Phased_array
- https://en.wikipedia.org/wiki/Smart_antenna
- https://en.wikipedia.org/wiki/Multiple-input_multiple-output_communications
- https://en.wikipedia.org/wiki/Diversity_combining
- https://en.wikipedia.org/wiki/Maximal-ratio_combining
- https://en.wikipedia.org/wiki/Orthogonal_frequency-division_multiplexing
- https://en.wikipedia.org/wiki/Orthogonal_frequency-division_multiple_access

Student Questions

Acronyms

BPSK	Binary Phase-Shift Keying
BS	Base Station
dB	DeciBels
dBi	DeciBels Intrinsic
dBm	DeciBels milliwatt
DFT	Discrete Fourier Transform
DMA	Direct Memory Access
DSP	Digital Signal Processing
DVB-H	Digital Video Broadcast handheld
FDMA	Frequency Division Multiple Access
FFT	Fast Fourier Transform
IDFT	Inverse Discrete Fourier Transform
IFFT	Inverse Fast Fourier Transform
ISI	Inter-symbol interference
kHz	Kilo Hertz
LoS	Line of Sight

Student Questions

Acronyms (Cont)

- MHz Mega Hertz
- MIMO Multiple Input Multiple Output
- MS Mobile Station
- OFDM Orthogonal Frequency Division Multiplexing
- OFDMA Orthogonal Frequency Division Multiple Access
- QAM Quadrature Amplitude Modulation
- QPSK Quadrature Phase-Shift Keying
- RF Radio Frequency
- SNR Signal to Noise Ratio
- SS Subscriber Station
- TDMA Time Division Multiple Access

Student Questions

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Raj Jain
http://rajjain.com

http://www.cse.wustl.edu/~jain/cse574-20/j_04wsp.htm

Student Questions

Related Modules

CSE567M: Computer Systems Analysis (Spring 2013), https://www.youtube.com/playlist?list=PLjGG94etKypJEKjNAa1n_1X0bWWNyZcof

CSE473S: Introduction to Computer Networks (Fall 2011), https://www.youtube.com/playlist?list=PLjGG94etKypJWOSPMh8Azcgy5e_10TiDw

Recent Advances in Networking (Spring 2013), https://www.youtube.com/playlist?list=PLjGG94etKypLHyBN8mOgwJLHD2FFIMGq5

CSE571S: Network Security (Fall 2011), https://www.youtube.com/playlist?list=PLjGG94etKypKvzfVtutHcPFJXumyyg93u

Video Podcasts of Prof. Raj Jain's Lectures, https://www.youtube.com/channel/UCN4-5wzNP9-ruOzQMs-8NUw

Student Questions