# **Introduction to Wireless Signal Propagation**



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- 1. Reflection, Diffraction, Scattering
- 2. Fading, Shadowing, multipath
- 3. Fresnel Zones
- 4. Multi-Antenna Systems, Beam forming, MIMO
- 5. OFDM

Note: This is the 2<sup>nd</sup> in a series of 2 lectures on wireless physical layer. Modulation, coding, Shannon's theorem, etc were discussed in the other lecture.

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## **Wireless Radio Channel**

- □ Path loss: Depends upon distance and frequency
- Noise
- □ Shadowing: Obstructions
- □ Frequency Dispersion (Doppler Spread) due to motion
- □ Interference
- □ Multipath: Multiple reflected waves
- □ Inter-symbol interference (ISI) due to dispersion



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#### Antenna

- □ Transmitter converts electrical energy to electromagnetic waves
- □ Receiver converts electromagnetic waves to electrical energy
- □ Same antenna is used for transmission and reception
- Omni-Directional: Power radiated in all directions
- Directional: Most power in the desired direction
- □ Isotropic antenna: Radiates in all directions equally
- Antenna Gain = Power at particular point/Power with Isotropic Expressed in dBi



Omni-Directional

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 $P_r = P_t G_t G_r (\lambda/4\pi d)^2$ 



Directional



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#### **Reflection, Diffraction and Scattering (Cont)**

**Reflection**: Surface large relative to wavelength of signal

- May have phase shift from original
- May cancel out original or increase it
- **Diffraction**: Edge of impenetrable body that is large relative to  $\lambda$ 
  - May receive signal even if no line of sight (LOS) to transmitter

#### □ Scattering

- > Obstacle size on order of wavelength. Lamp posts etc.
- □ If LOS, diffracted and scattered signals not significant
  - > Reflected signals may be
- If no LOS, diffraction and scattering are primary means of reception

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- Power profile of the received signal can be obtained by convolving the power profile of the transmitted signal with the impulse response of the channel.
- □ Convolution in time = multiplication in frequency
- □ Signal *x*, after propagation through the channel *H* becomes *y*: y(f)=H(f)x(f)+n(f)
- □ Here H(f) is **channel response**, and n(f) is the noise. Note that *x*, *y*, *H*, and *n* are all functions of the signal frequency *f*. Washington University in St. Louis <u>http://www.cse.wustl.edu/~jain/cse574-18/</u> ©2018 Rai Jain

#### **Path Loss**

Power is distributed equally to spherical area 4π d<sup>2</sup>
 The received power depends upon the wavelength
 If the Receiver collects power from area A<sub>R</sub>:

$$P_R = P_T G_T \frac{1}{4\pi d^2} A_R$$

Receiving Antenna Gain

$$G_R = \frac{4\pi}{\lambda^2} A_R$$

$$P_R = P_T G_T G_R \left(\frac{\lambda}{4\pi d}\right)^2$$

□ This is known as **Frii's Law**. Attenuation in free space increases with frequency.





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#### d<sup>-4</sup> Power Law



Using a two-ray model

$$P_R = P_T G_T G_R \left(\frac{h_t h_r}{d^2}\right)^2$$

- □ Here,  $h_T$  and  $h_R$  are heights of transmit and receive antennas
- □ It is valid for distances larger than

$$d_{\rm break} = 4h_T h_R / \lambda$$

- Note that the received power becomes independent of the frequency.
- Measured results show n=1.5 to 5.5. Typically 4.

#### **Small Scale Fading**

□ The signal amplitude can change by moving a few inches ⇒ Small scale fading







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- Draw an ellipsoid with BS and MS as Foci
- □ All points on ellipsoid have the same BS-MS run length
- □ Fresnel ellipsoids = Ellipsoids for which run length =  $LoS + i\lambda/2$
- □ At the Fresnel ellipsoids results in a phase shift of i\pi
- Radius of the *i*<sup>th</sup> ellipsoid at distance  $d_T$  from the transmitter and  $d_R$  from the receiver is  $\sqrt{1\lambda d_T d_R}$

$$\sqrt{\frac{1\lambda d_T d_R}{d_T + d_R}}$$

Free space (d<sup>2</sup>) law is followed up to the distance at which the first Fresnel Ellipsoid touches the ground

### **Multi-Antenna Systems**

- **Receiver** Diversity
- **Transmitter Diversity**
- Beam forming
- MIMO

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- User multiple receive antenna
- Selection combining: Select antenna with highest SNR
- Threshold combining: Select the first antenna with SNR above a threshold
- Maximal Ratio Combining: Phase is adjusted so that all signals have the same phase. Then weighted sum is used to maximize SNR Washington University in St. Louis
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- Use multiple antennas to transmit the signal Ample space, power, and processing capacity at the transmitter (but not at the receiver).
- If the channel is known, phase each component and weight it before transmission so that they arrive in phase at the receiver and maximize SNR
- □ If the channel is not known, use space time block codes
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- Phased Antenna Arrays: Receive the same signal using multiple antennas
- □ By phase-shifting various received signals and then summing ⇒ Focus on a narrow directional beam
- □ Digital Signal Processing (DSP) is used for signal processing ⇒ Self-aligning

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# MIMO



- Multiple Input Multiple Output
- □ RF chain for each antenna
  - $\Rightarrow$  Simultaneous reception or transmission of multiple streams



#### 802.16e at 2.5 GHz, 10 MHz TDD, D:U=2:1

T:R	1x1	1x2	2x2	2x4	4x2	4x4
b/Hz	1.2	1.8	2.8	4.4	3.7	5.1

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#### **Multiple Access Methods**



Source: Nortel

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## **OFDM**

- Orthogonal Frequency Division Multiplexing
- □ Ten 100 kHz channels are better than one 1 MHz Channel ⇒ Multi-carrier modulation  $\square$





- □ Frequency band is divided into 256 or more sub-bands. Orthogonal ⇒ Peak of one at null of others
- Each carrier is modulated with a BPSK, QPSK, 16-QAM, 64-QAM etc depending on the noise (Frequency selective fading)
- Used in 802.11a/g, 802.16,
   Digital Video Broadcast handheld (DVB-H) <sup>und</sup>
- Easy to implement using FFT/IFFT



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Freq

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## **Advantages of OFDM**

- □ Easy to implement using FFT/IFFT
- Computational complexity = O(B log BT) compared to previous O(B<sup>2</sup>T) for Equalization. Here B is the bandwidth and T is the delay spread.
- Graceful degradation if excess delay
- □ Robustness against frequency selective burst errors
- □ Allows adaptive modulation and coding of subcarriers
- Robust against narrowband interference (affecting only some subcarriers)
- Allows pilot subcarriers for channel estimation

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#### **OFDM: Design considerations**

- Large number of carriers ⇒ Smaller data rate per carrier
   ⇒ Larger symbol duration ⇒ Less inter-symbol interference
- □ Reduced subcarrier spacing ⇒ Increased inter-carrier interference due to Doppler spread in mobile applications
- Easily implemented as Inverse Discrete Fourier Transform (IDFT) of data symbol block
- Fast Fourier Transform (FFT) is a computationally efficient way of computing DFT



#### **OFDMA**

- Orthogonal Frequency Division <u>Multiple Access</u>
- □ Each user has a subset of subcarriers for a few slots
- □ OFDM systems use TDMA
- □ OFDMA allows Time+Freq DMA  $\Rightarrow$  2D Scheduling



# Scalable OFDMA (SOFDMA)

- □ OFDM symbol duration = f(subcarrier spacing)
- Subcarrier spacing = Frequency bandwidth/Number of subcarriers
- Frequency bandwidth=1.25 MHz, 3.5 MHz, 5 MHz, 10 MHz, 20 MHz, etc.
- Symbol duration affects higher layer operation
   ⇒ Keep symbol duration constant at 102.9 us
   ⇒ Keep subcarrier spacing 10.94 kHz
   ⇒ Number of subcarriers ∞ Frequency bandwidth This is known as scalable OFDMA

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# **Effect of Frequency (Cont)**

- □ Lower frequencies have longer reach
  - $\Rightarrow$  Longer Cell Radius
  - $\Rightarrow$  Good for rural areas
  - $\Rightarrow$  Smaller number of towers
  - $\Rightarrow$  Longer battery life
- ❑ Lower frequencies require larger antenna and antenna spacing
   ⇒ MIMO difficult particularly on mobile devices
- □ Lower frequencies  $\Rightarrow$  Smaller channel width  $\Rightarrow$  Need aggressive MCS, e.g., 256-QAM
- Doppler shift = vf/c = Velocity ×Frequency/(speed of light)
   ⇒ Lower Doppler spread at lower frequencies
- □ Mobility  $\Rightarrow$  Below 10 GHz

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- 1. Path loss increase at a power of 2 to 5.5 with distance.
- 2. Fading = Changes in power changes in position
- 3. Fresnel zones = Ellipsoid with distance of LoS+ $i\lambda/2$ Any obstruction of the first zone will increase path loss
- 4. Multiple Antennas: Receive diversity, transmit diversity, Smart Antenna, MIMO
- 5. OFDM splits a band in to many orthogonal subcarriers. OFDMA = FDMA + TDMA

#### **Homework 4**

- A. Determine the mean received power at a SS. The channel between a base station at 14 m and the subscriber stations at 4m at a distance of 500m. The Transmitter and Receiver antenna gains are 10dB and 5 dB respectively. Use a power exponent of 4. Transmitted power is 30 dBm. Do All calculations using dB.
- B. With a subcarrier spacing of 10 kHz, how many subcarriers will be used in a system with 8 MHz channel bandwidth and what size FFT will be used?
- C. In a scalable OFDMA system, the number of carriers for 10 MHz channel is 1024. How many carriers will be used if the channel was 1.25 MHz, 5 MHz, or 8.75 MHz.

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### **Reading List**

- Jim Geier, "Radio Wave Fundamentals," Chapter 2 in his book "Designing and Deploying 802.11 Wireless Networks: A Practical Guide to Implementing 802.11n and 802.11ac Wireless Networks, Second Edition," Cisco Press, May 2015, 600 pp., ISBN:1-58714-430-1 (Safari Book), Chapter 2.
- Raj Jain, "Channel Models: A Tutorial," WiMAX Forum AATG, February 2007, first 7 of 21 pages, http://www.cse.wustl.edu/~jain/wimax/channel model tutorial.htm
- □ Jim Geier, "Wireless Networks first-step," Cisco Press, August 2004, 264 pp., ISBN:1-58720-111-9 (Safari Book), Chapter 3.
- Steve Rackley, "Wireless Networking Technology," Newnes, March 2007, 416 pp., ISBN:0-7506-6788-5 (Safari Book), Chapter 4.
- Stephan Jones; Ronald J. Kovac; Frank M. Groom, "Introduction to Communications Technologies, 3rd Edition," CRC Press, July 2015, 364 pp., ISBN:978-1-4987-0295-9 (Safari Book), Chapters 3 and 4.

# Wikipedia Links

- □ <u>https://en.wikipedia.org/wiki/Omnidirectional\_antenna</u>
- □ <u>https://en.wikipedia.org/wiki/Antenna\_gain</u>
- □ <u>https://en.wikipedia.org/wiki/Equivalent\_isotropically\_radiated\_power</u>
- □ <u>https://en.wikipedia.org/wiki/High-gain\_antenna</u>
- □ <u>https://en.wikipedia.org/wiki/Signal\_reflection</u>
- https://en.wikipedia.org/wiki/Scattering
- □ <u>https://en.wikipedia.org/wiki/Path\_loss</u>
- <u>https://en.wikipedia.org/wiki/Free-space\_path\_loss</u>
- □ <u>https://en.wikipedia.org/wiki/Log-distance\_path\_loss\_model</u>
- □ <u>https://en.wikipedia.org/wiki/Multipath\_propagation</u>
- □ <u>https://en.wikipedia.org/wiki/Multipath\_interference</u>
- <u>https://en.wikipedia.org/wiki/Intersymbol\_interference</u>
- □ <u>https://en.wikipedia.org/wiki/Fading</u>
- □ <u>https://en.wikipedia.org/wiki/Shadow\_fading</u>
- https://en.wikipedia.org/wiki/Fresnel\_zone

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# Wikipedia Links (Cont)

- □ <u>https://en.wikipedia.org/wiki/Antenna\_diversity</u>
- □ <u>https://en.wikipedia.org/wiki/Beamforming</u>
- □ <u>https://en.wikipedia.org/wiki/Antenna\_array\_(electromagnetic)</u>
- □ <u>https://en.wikipedia.org/wiki/Phased\_array</u>
- □ <u>https://en.wikipedia.org/wiki/Smart\_antenna</u>
- <u>https://en.wikipedia.org/wiki/Multiple-input\_multiple-output\_communications</u>
- □ <u>https://en.wikipedia.org/wiki/Diversity\_combining</u>
- □ <u>https://en.wikipedia.org/wiki/Maximal-ratio\_combining</u>
- □ <u>https://en.wikipedia.org/wiki/Orthogonal\_frequency-division\_multiplexing</u>
- <u>https://en.wikipedia.org/wiki/Orthogonal\_frequency-division\_multiple\_access</u>

#### Acronyms

- **BPSK** Binary Phase-Shift Keying
- **BS** Base Station
- □ dB DeciBels
- □ dBi DeciBels Intrinsic
- □ dBm DeciBels milliwatt
- DFT Discrete Fourier Transform
- DMA Direct Memory Access
- DSP Digital Signal Processing
- DVB-H Digital Video Broadcast handheld
- **G** FDMA Frequency Division Multiple Access
- □ FFT Fast Fourier Transform
- □ IDFT Inverse Discrete Fourier Transform
- □ IFFT Inverse Fast Fourier Transform
- □ ISI Inter-symbol interference
- □ kHz Kilo Hertz
- □ LoS Line of Sight

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### Acronyms (Cont)

- □ MHz Mega Hertz
- MIMO Multiple Input Multiple Output
- MS Mobile Station
- OFDM Orthogonal Frequency Division Multiplexing
- OFDMA Orthogonal Frequency Division Multiple Access
- QAMQuadrature Amplitude Modulation
- QPSK Quadrature Phase-Shift Keying
- □ RF Radio Frequency
- □ SNR Signal to Noise Ratio
- □ SS Subscriber Station
- **TDMA** Time Division Multiple Access

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### **Related Modules**



CSE567M: Computer Systems Analysis (Spring 2013), https://www.youtube.com/playlist?list=PLjGG94etKypJEKjNAa1n\_1X0bWWNyZcof

CSE473S: Introduction to Computer Networks (Fall 2011), https://www.youtube.com/playlist?list=PLjGG94etKypJWOSPMh8Azcgy5e\_10TiDw





Recent Advances in Networking (Spring 2013),

https://www.youtube.com/playlist?list=PLjGG94etKypLHyBN8mOgwJLHD2FFIMGq5

CSE571S: Network Security (Fall 2011),

https://www.youtube.com/playlist?list=PLjGG94etKypKvzfVtutHcPFJXumyyg93u





Video Podcasts of Prof. Raj Jain's Lectures,

https://www.youtube.com/channel/UCN4-5wzNP9-ruOzQMs-8NUw

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