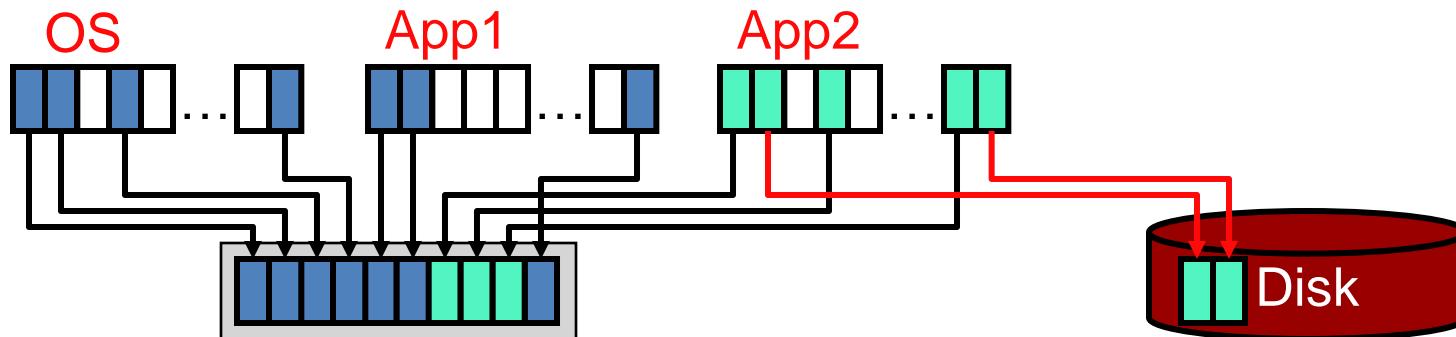
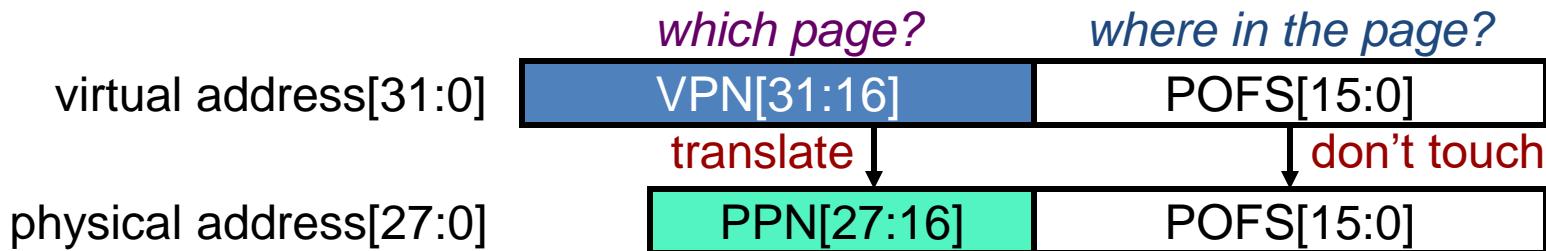


# Virtual Memory: The Basics

- Programs use **virtual addresses (VA)**
  - VA size (N) aka machine size (e.g., Core 2 Duo: 48-bit)
- Memory uses **physical addresses (PA)**
  - PA size (M) typically  $M < N$ , especially if  $N=64$
  - $2^M$  is most physical memory machine supports
- VA→PA at **page** granularity (VP→PP)
  - Mapping need not preserve contiguity
  - VP need not be mapped to any PP
  - Unmapped VPs live on disk (swap) or nowhere (if not yet touched)



# Address Translation



- VA→PA mapping called **address translation**
  - Split VA into **virtual page number (VPN)** & **page offset (POFS)**
  - Translate VPN into **physical page number (PPN)**
  - POFS is not translated
  - VA→PA = [VPN, POFS] → [PPN, POFS]

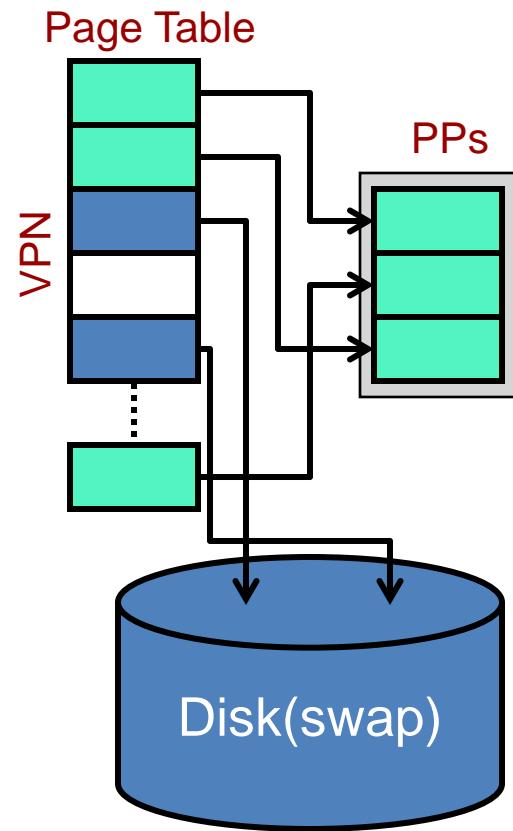
Example above

- 64KB per page → 16-bit POFS  $(2^{16}=64K)$
- 32-bit machine → 32-bit VA → 16-bit VPN  $32-16=16$
- Max. 256MB memory → 28-bit PA → 12-bit PPN  $28-16=12$   
 $(2^{28}=256M)$

# Address Translation Mechanics I

- How are addresses translated?
  - In sw (for now) but with hardware acceleration (a little later)
- Each process allocated a **page table (PT)**
  - **In-memory data structure constructed by OS**
  - Maps VPs to PPs or to disk (swap) addresses
    - VP entries empty if page never referenced
  - Translation is table lookup

```
struct {  
    int ppn;  
    int is_valid, is_dirty, is_swapped;  
} PTE;  
struct PTE page_table[NUM_VIRTUAL_PAGES];  
  
int translate(int vpn) {  
    if (page_table[vpn].is_valid)  
        return page_table[vpn].ppn;  
}
```



# Page Table Size

---

**How big is a page table on the following machine?**

**Given:**

- 32-bit machine
- 4KB per page
- 4B page table entries (PTEs) (see struct definition, prev slide)

**Can determine:**

- 32-bit machine → 32-bit VA → 4GB virtual memory ( $2^{32}=4G$ )
- 4GB virtual memory / 4KB page size → 1M VPs
- Each VP needs a PTE: 1M VPs → 1M PTEs
- 1M PTEs x 4B-per-PTE → **4MB**
  
- How big would the page table be with 64KB pages?
- How big would it be for a 64-bit machine?
- Page tables can get *big* (see next slides)

# Page Table Size

---

**How big is a page table on the following machine?**

**Given:**

- 32-bit machine
- 64KB per page
- 4B page table entries (PTEs)

**Can determine:**

- 32-bit machine → 32-bit VA → 4GB virtual memory ( $2^{32}=4G$ )
- 4GB virtual memory / 64KB page size → 64K VPs
- Each VP needs a PTE: 64K VPs → 64K PTEs
- 64K PTEs x 4B-per-PTE → **256KB**
- Not so bad. What about 64-bit machine?

# Page Table Size

---

**How big is a page table on the following machine?**

**Given:**

- 64-bit machine
- 64KB per page

**Can determine:**

- 64-bit machine → 64-bit VA →  
9,223,372,036,854,775,807B virtual memory
- 64KB page size → > 100 trillion VPs !!!!

# Multi-Level Page Table (PT)

---

One way: **multi-level page tables**

- Tree of page tables
- Lowest-level tables hold PTEs
- Upper-level tables hold pointers to lower-level tables
- Different parts of VPN used to index different levels

Example: two-level page table for 32-bit machine w/ 4KB pages

- Compute number of pages needed for lowest-level (PTEs)
  - 4KB page size / 4B-per-PTE → can hold 1K PTEs per page
  - 1M PTEs / (1K PTEs/page) → 1K pages
- Compute # of pages needed for upper-level (pointers)
  - 1K lowest-level pages → 1K pointers
  - 1K pointers x 32-bit VA → 4KB → 1 upper level page

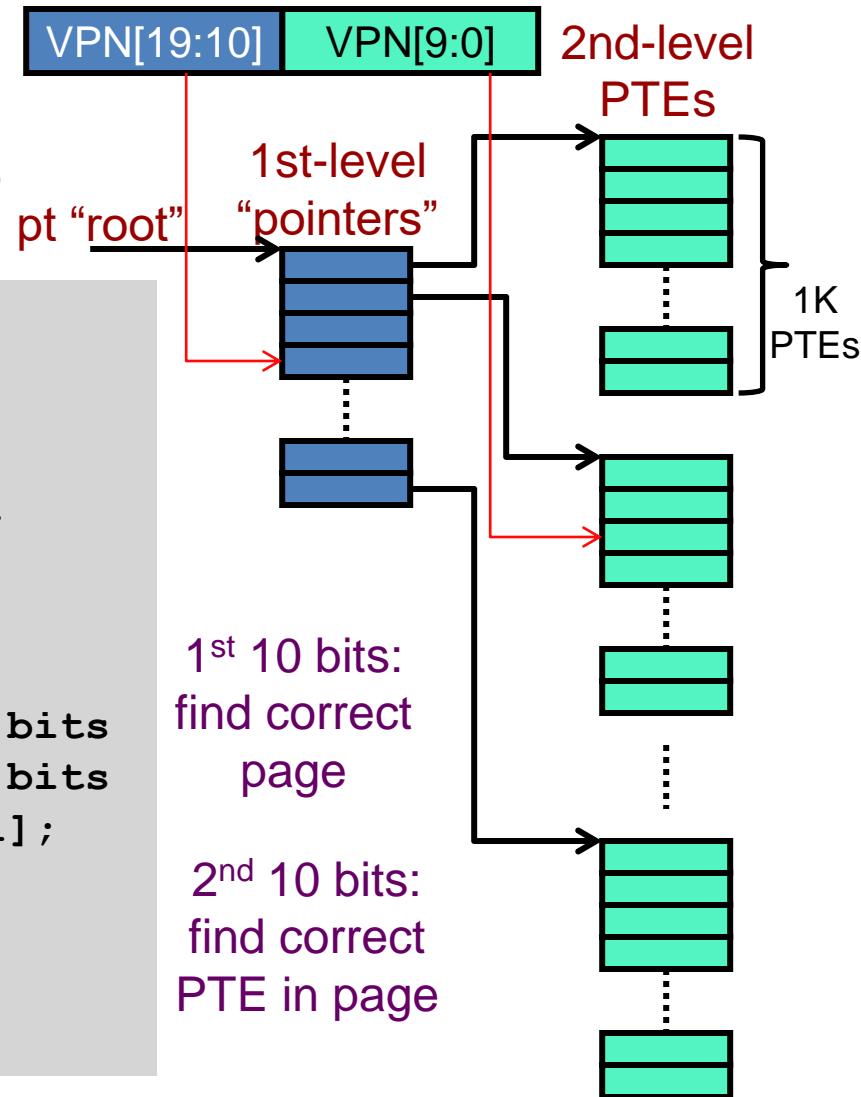
# Multi-Level Page Table (PT)

20-bit VPN

- Upper 10 bits index 1st-level table
- Lower 10 bits index 2nd-level table

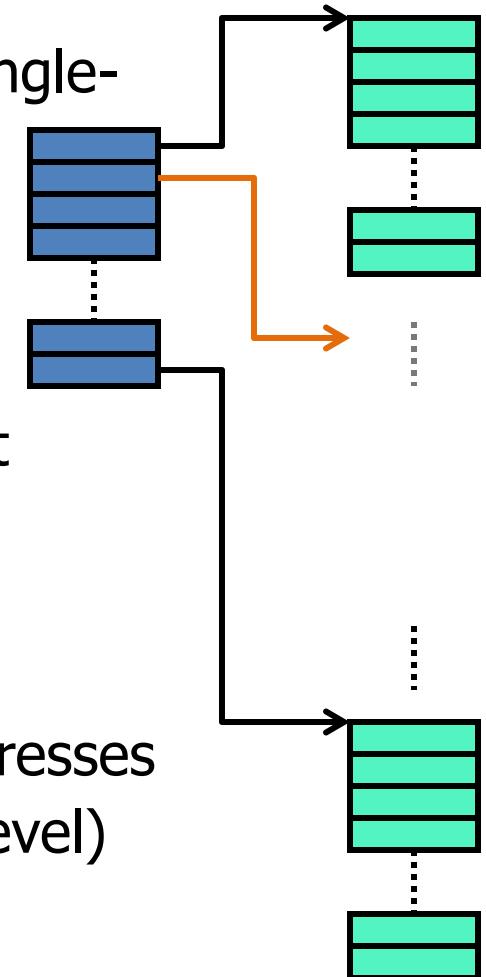
```
struct {  
    int ppn;  
    int is_valid, is_dirty, is_swapped;  
} PTE;  
struct { struct PTE ptes[1024]; } L2PT;  
struct L2PT *page_table[1024];
```

```
int translate(int vpn) {  
    index1 = (vpn >> 10); // upper 10 bits  
    index2 = (vpn & 0x3ff); // lower 10 bits  
    struct L2PT *l2pt = page_table[index1];  
    if (l2pt != NULL &&  
        l2pt->ptes[index2].is_valid)  
        return l2pt->ptes[index2].ppn;  
}
```



# Multi-Level Page Table (PT)

- Have we saved any space?
  - Isn't total size of 2nd level tables same as single-level table (*i.e.*, 4MB)?
  - Yes, but...
- Large virtual address regions unused
  - Corresponding 2<sup>nd</sup>-level tables need not exist
  - Corresponding 1<sup>st</sup>-level pointers are null
- Example: 2MB code, 64KB stack, 16MB heap
  - Each 2<sup>nd</sup>-level table maps 4MB of virtual addresses
  - 1 for code, 1 for stack, 4 for heap, (+1 1st-level)
  - 7 total pages = 28KB (much less than 4MB)



# Page-Level Protection

---

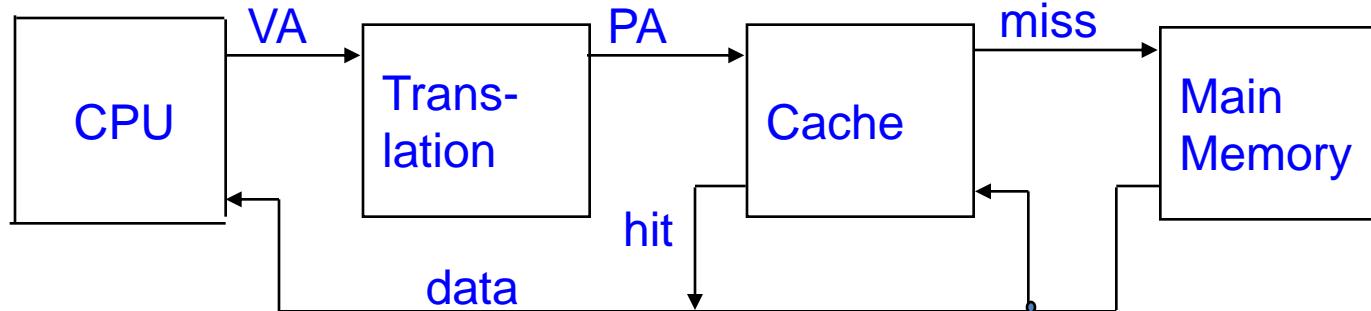
- **Page-level protection**

- Piggy-back page-table mechanism
- Map VPN to PPN + Read/Write/Execute permission bits
- Attempt to execute data, to write read-only data?
  - Exception → OS terminates program
- Useful (for OS itself actually)

```
struct {
    int ppn;
    int is_valid, is_dirty, is_swapped, permissions;
} PTE;
struct PTE page_table[NUM_VIRTUAL_PAGES];

int translate(int vpn, int action) {
    if (page_table[vpn].is_valid &&
        !(page_table [vpn].permissions & action)) kill;
    ...
}
```

# Integrating VM and Cache



- Most Caches “Physically Addressed”
  - Accessed by physical addresses
  - Allows multiple processes to have blocks in cache at same time
  - Allows multiple processes to share pages
  - Cache doesn’t need to be concerned with protection issues
    - Access rights checked as part of address translation
- Perform Address Translation Before Cache Lookup
  - But this could involve a memory access itself (of the PTE)
  - Of course, page table entries can also become cached

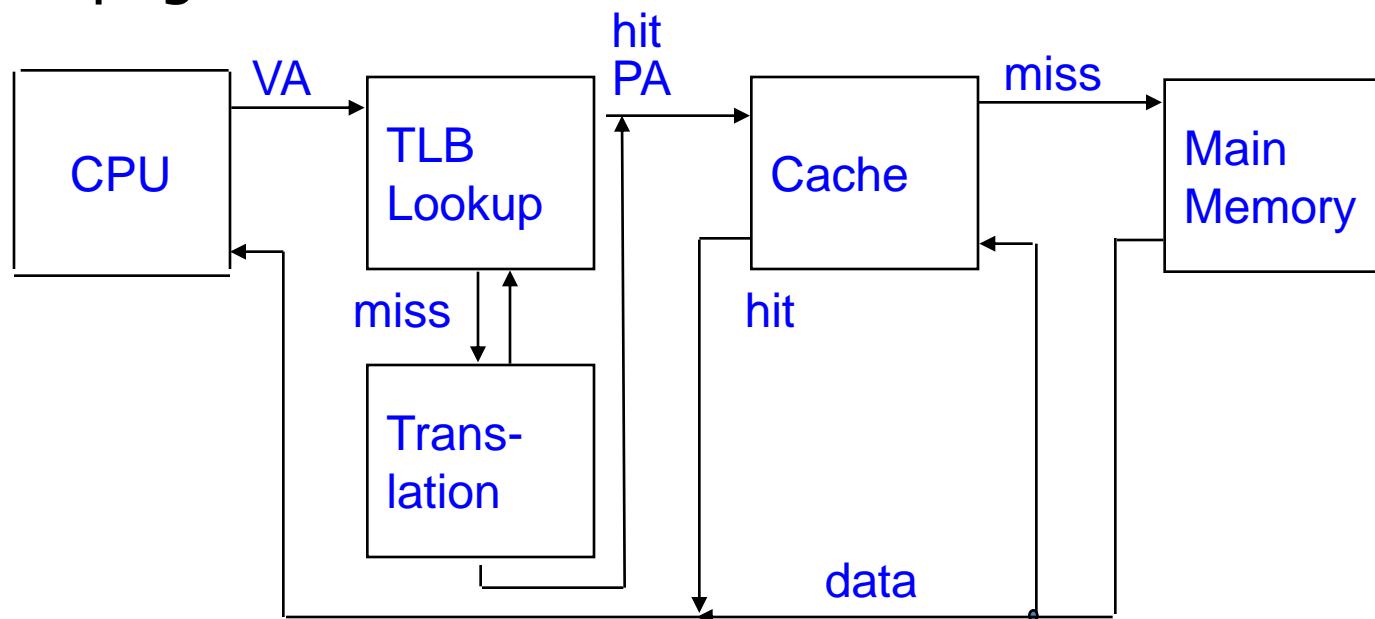
# Address Translation Mechanics II

---

- Conceptually
  - Translate VA to PA before every cache access
  - Walk the page table before every load/store/insn-fetch
    - Would be terribly inefficient (even in hardware)
- In reality
  - Translation Lookaside Buffer (**TLB**): cache translations
  - Only walk page table on TLB miss
- Hardware truisms
  - Functionality problem? Add indirection (*e.g.*, VM)
  - Performance problem? Add cache (*e.g.*, TLB)

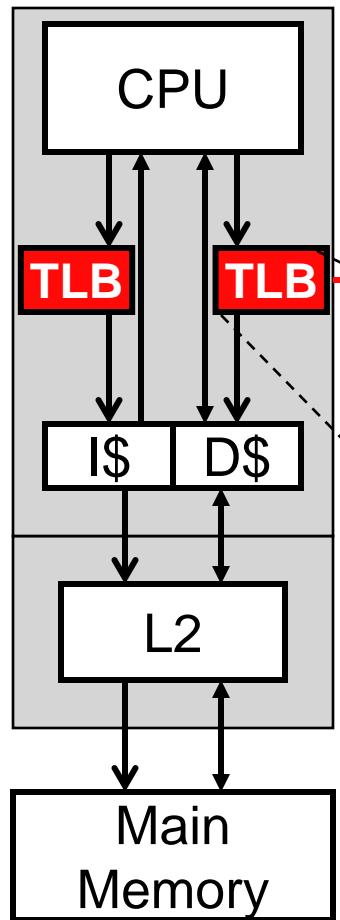
# Speeding up Translation with a TLB

- “Translation Lookaside Buffer” (TLB)
  - Small hw cache in MMU (memory management unit)
  - Maps virtual page numbers to physical page numbers
  - Contains complete page table entries for small number of pages

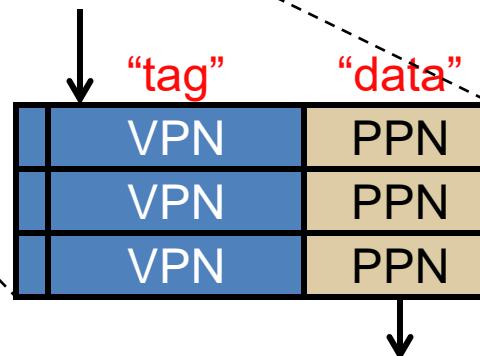


# Translation Lookaside Buffer

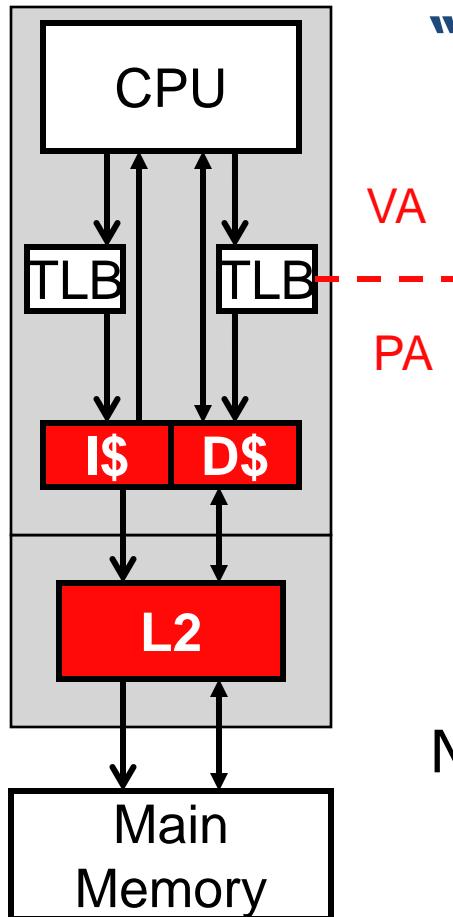
## Translation lookaside buffer (TLB)



- Small cache: 16–64 entries
- Associative (4+ way or fully associative)
  - + Exploits temporal locality in page table
- What if an entry isn't found in the TLB?
  - Invoke TLB miss handler



# Serial TLB & Cache Access



## “Physical” caches

- Indexed and tagged by **physical addresses**
- + Natural, “lazy” sharing of caches between apps/OS
  - VM ensures isolation (via **physical addresses**)
  - No need to do anything on context switches
  - Multi-threading works too
- + Cached inter-process communication works
  - Single copy indexed by physical address
- Slow: adds at least one cycle to  $t_{hit}$

Note: **TLBs are by definition “virtual”**

- Indexed and tagged by **virtual addresses**
- Flush across context switches
- Or extend with process identifier tags (x86)

# Parallel TLB & Cache Access

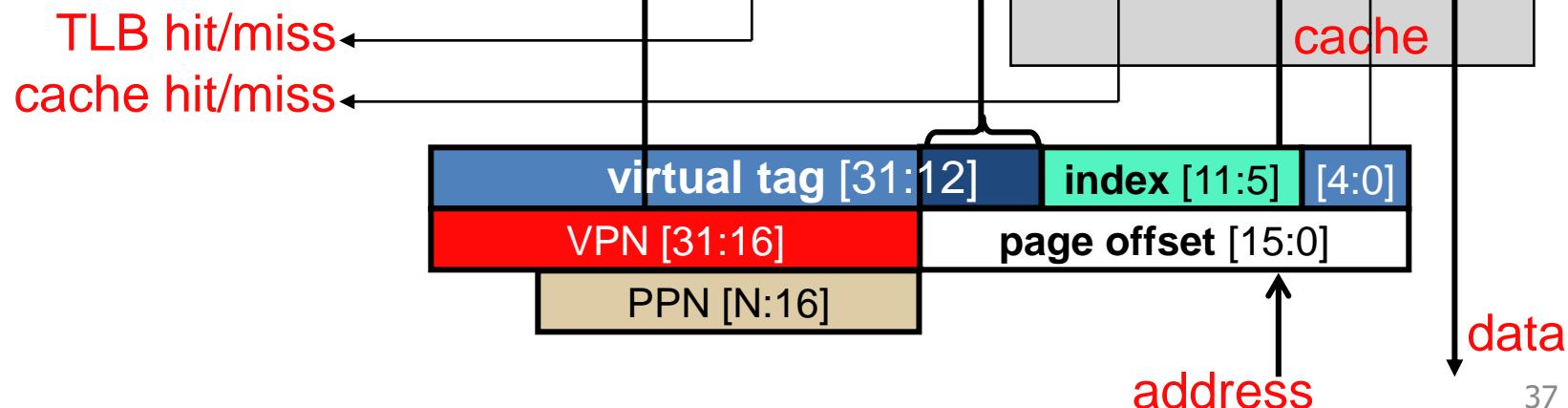
Two ways to look at VA

- Cache: tag+index+offset
- TLB: **VPN**+page offset

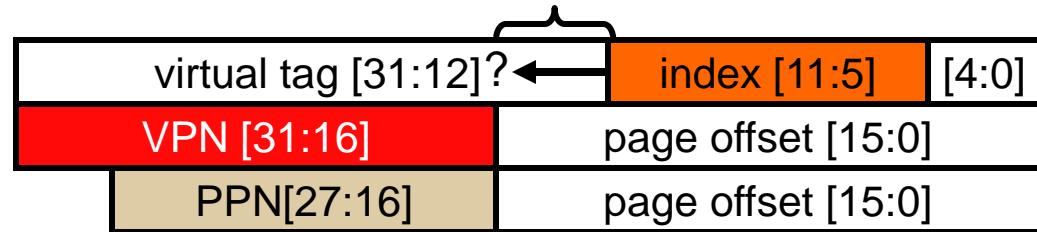
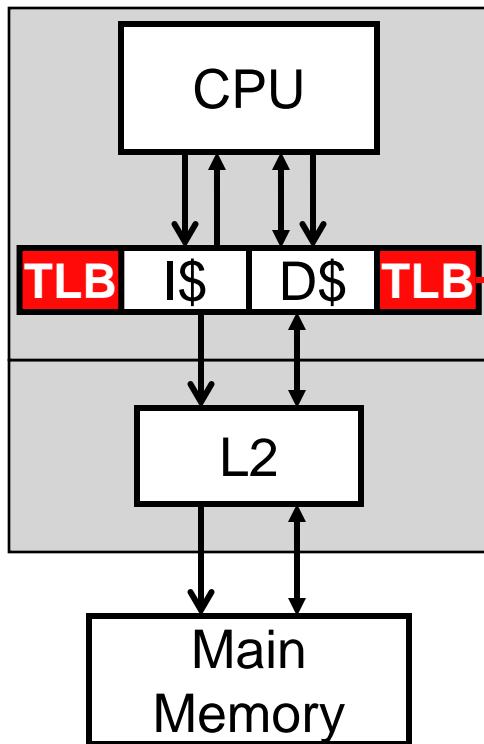
Parallel cache/TLB...

- If address translation doesn't change index

→ VPN/index  
must not overlap



# Parallel TLB & Cache Access



What about parallel access?

- Only if...  
VA - **(cache size) / (associativity) ≤ page size**
  - Index bits same in virtual & physical addresses!
- Access TLB in parallel with cache
  - Cache access needs tag only at very end
    - + Fast: no additional  $t_{hit}$  cycles
    - + No context-switching/aliasing problems
  - Dominant organization used today
- Example: Core 2, 4KB pages, 32KB, 8-way SA L1 data cache
  - Implication: *associativity allows bigger caches*

# TLB Organization

---

- **Like caches:** TLBs also have ABCs
  - Capacity
  - Associativity (At least 4-way associative, fully-associative common)
  - What does it mean for a TLB to have a block size of two?
    - Two consecutive VPs share a single tag
  - **Like caches:** there can be L2 TLBs
- Example: AMD Opteron
  - 32-entry fully-assoc. TLBs, 512-entry 4-way L2 TLB (insn & data)
  - 4KB pages, 48-bit virtual addresses, four-level page table
- **Rule of thumb:** TLB should “cover” on-chip L2 cache contents
  - In other words: (#PTEs in TLB)  $\times$  page size  $\geq$  L2 size
  - Why? Consider relative miss latency in each...

# TLB Misses

---

- **TLB miss:** translation not in TLB, but in page table
  - Two ways to “fill” it, both relatively fast
- **Software-managed TLB:** *e.g.*, Alpha, MIPS, ARM
  - Short (~10 insn) OS routine walks page table, updates TLB
    - + Keeps page table format flexible
    - Latency: one or two memory accesses + OS call (pipeline flush)
- **Hardware-managed TLB:** *e.g.*, x86
  - Page table root in hardware register, hardware “walks” table
    - + Latency: saves cost of OS call (avoids pipeline flush)
    - Page table format is hard-coded
- Trend is towards hardware TLB miss handler

# Page Faults

---

**Page fault:** PTE not in TLB or page table → page not in memory

- Or no valid mapping → segmentation fault
- Starts out as a TLB miss, detected by OS/hardware handler

**OS software routine:**

- Choose a physical page to replace
  - “**Working set**”: refined LRU, tracks active page usage
- If dirty, write to disk
- Read missing page from disk
  - Takes so long ( $\sim 10\text{ms}$ ), OS schedules another task
- Treat like a normal TLB miss from here

# Summary

---

- OS virtualizes memory and I/O devices
- Virtual memory
  - “infinite” memory, isolation, protection, inter-process communication
  - Page tables
  - Translation buffers
    - Parallel vs. serial access, interaction with caching
  - Page faults