After you have successfully completed your implementation of the hash table, answer the following questions.

First, for each of the five methods you implemented, describe briefly (in three sentences or less) how it works. Did it use any instance variables of the class, and if so, which ones? Are any helper methods called by the method (either of your own creation or in the original codebase), and if so, which ones and what do they do? In particular, describe your computation to map hashcodes to indices in the table for the `toIndex` method.

The methods that you should describe are:

1. `public StringTable(int nBuckets);`
2. `public boolean insert(Record r);`
3. `public Record find(String key);`
4. `public void remove(String key);`
5. `private int toIndex(int hashcode);`

Now answer the following additional questions:

6. Java linked lists, which you used to implement each hash bucket, have both head and tail pointers. Hence, it does not matter to the cost of insertion whether you use `add()` or `addFirst()` to insert a new item.

   Assume that the `find()` method traverses a bucket starting from the head of its list. If the person using your hash table frequently accesses the most recently inserted item(s), which of these two insertion methods (i.e., `add()` or `addFirst()`) is likely to yield better performance, and why? What if the user frequently accesses the least recently inserted item(s)?

7. Our hash table is allocated with a fixed number of buckets. If we insert a bunch of values, the load factor of the table (number of items over number of buckets) can grow without bound. We’d instead like to maintain the table’s load factor $\leq$ some constant $L$, no matter how big it grows.

   Why would maintaining a fixed maximum load factor help the performance of the table? What is the average-case running time of table operations if a fixed maximum load factor is used?

8. One way to decrease the table’s load factor is to make it bigger; that is, we create a new table with more buckets and then transfer the items from the old table to the new one.

   Sketch pseudocode for this operation. Assume we have an existing array $B$ of $m$ buckets, and we are transferring its contents to a new array $B'$ of $m' > m$ buckets. Be sure to specify which value, $m$ or $m'$, is used by your `toIndex()` function.

9. How much time does it take (asymptotically, on average) to transfer $n$ elements from the old to the new table, assuming simple uniform hashing? Be sure to explain where your answer comes from.
10. Describe a strategy for deciding when to allocate a new table, and what size the new table should be, so as to keep the maximum load factor $\leq L$ while maintaining an amortized average-case cost of insertion $\Theta(1)$. (Hint: remember your first couple of studios!) Justify that your answer meets these constraints.